## Functions, Domain and Range Overview

## The test for a function (from a graph)

A relation is any set of ordered pairs ( $\mathrm{x}, \mathrm{y}$ ). A function is a special type of relation. A function is a relation where each $x$-value has only one $y$-value. The vertical line test can be used to determine if the graph of a relation is a function. If a vertical line passes through more than one point anywhere on the graph, then it is not a function. See the examples below:


NOT a function: fails vertical line test


IS a function: passes vertical line test


NOT a function: fails vertical line test


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The test for a function from its equation

1. A relation is NOT A FUNCTION if there exists:
(i) $\underline{a}$ " $\pm$ " symbol on an $x$-expression or
(ii) even power of $y$ or
(iii) y -variable expression inside absolute value symbols or
(iv) inequality symbols $(\langle\rangle,, \leq, \geq)$

## Examples of how each of these 4 cases fail the vertical line test


(i) $y= \pm \sqrt{x+2}$
(ii)

$x=y 2$ (iii) $x=|y|$

(iv)

$y \geq x$

## 2. In ALL other cases the relation IS A FUNCTION. <br> Determining the domain of a function from its equation

Domain deals with the acceptable values for the $x$ variable and Range deals with the subsequent values for the $y$ variable. Below are some examples that show some of the various types of problems most students encounter. Mainly two things limit your domain, a fraction and an even indexed radical. The range is probably easiest to determine when looking at a graph of the function.


