Functions, Domain and Range Overview

The test for a function (from a graph)

A *relation* is any set of ordered pairs (x,y). A *function* is a special type of relation. A *function* is a relation where each x-value has only one y-value. The *vertical line test* can be used to determine if the graph of a relation is a function. If a vertical line passes through more than one point <u>anywhere</u> on the graph, then it is <u>not</u> a function. See the examples below:



NOT a function: fails vertical line test

NOT a function: fails vertical line test





IS a function: passes vertical line test



The test for a function from its equation

<u>1.</u> A relation is **NOT A FUNCTION** if there exists:

- (i) <u>a " \pm " symbol on an x-expression</u> or
- (ii) <u>even power of y</u> or
- (iii) <u>y-variable expression inside absolute value symbols</u> or
- (iv) <u>inequality symbols</u> $(< , > , \le , \ge)$

Examples of how each of these 4 cases fail the vertical line test



<u>2.</u> <u>In ALL other cases the relation IS A FUNCTION.</u> Determining the domain of a function from its equation

Domain deals with the acceptable values for the x variable and Range deals with the subsequent values for the y variable. Below are some examples that show some of the various types of problems most students encounter. Mainly two things limit your domain, a fraction and an even indexed radical. The range is probably easiest to determine when looking at a graph of the function.

