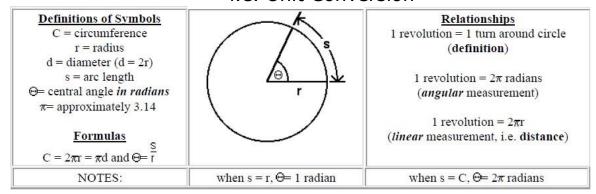
Finding Angular and Linear Speeds by Dimensional Analysis

i.e. Unit Conversion



EXAMPLES:

(Note CANCELLATION OF UNITS! Un-cancelled units are **boldfaced**.)

1. A phonograph record has a radius of 3 inches and revolves at 45 RPM. Find the linear speed of the outside edge of the record.

Solution: Use the fact that 1 revolution = 2 pi r:

$$\left(\frac{45 \text{ revolutions}}{1 \text{ minute}}\right) = \left(\frac{45 \text{ revolutions}}{1 \text{ minute}}\right) \cdot \left(\frac{2\pi(3) \text{ inches}}{1 \text{ Tevolution.}}\right) = (848.2 \frac{\text{inches}}{\text{minute}})$$

- 2. A car is traveling 60 mph. The diameter of the wheels is 3 ft.
 - a. Find the number of revolutions per minute the wheels are rotating.

Strategy: We need to convert
$$\frac{\text{mile}}{\text{hour}} \to \frac{\text{feet}}{\text{hour}} \to \frac{\text{feet}}{\text{minute}} \to \frac{\text{revolutions}}{\text{minute}}$$
so, we need three conversion ratios.

$$\begin{pmatrix} 60 & \frac{\text{miles}}{\text{hour}} \end{pmatrix} = \begin{pmatrix} 60 & \frac{\text{friiles}}{\text{hour}} \end{pmatrix} \cdot \begin{pmatrix} \frac{5280 \text{ feet}}{1 \text{ mile}} \end{pmatrix} \qquad \text{(since 1 mile = 5280 feet)}$$

$$\begin{pmatrix} 60 & \frac{\text{miles}}{\text{hour}} \end{pmatrix} \cdot \begin{pmatrix} \frac{5280 \text{ feet}}{1 \text{ mile}} \end{pmatrix} \cdot \begin{pmatrix} \frac{1 \text{ hour}}{60 \text{ minutes}} \end{pmatrix} \qquad \text{(since 1 hour = 60 minutes)}$$

$$\begin{pmatrix} 60 & \frac{\text{miles}}{\text{hour}} \end{pmatrix} \cdot \begin{pmatrix} \frac{5280 \text{ feet}}{1 \text{ mile}} \end{pmatrix} \cdot \begin{pmatrix} \frac{1 \text{ hour}}{60 \text{ minutes}} \end{pmatrix} \cdot \begin{pmatrix} \frac{1 \text{ revolution}}{2\pi (1.5) \text{ feet}} \end{pmatrix} = \begin{pmatrix} 560.2 & \frac{\text{revolutions}}{\text{minute}} \end{pmatrix}$$

b. What's the angular speed of the wheels in radians per minute?

$$\left(560.2 \frac{\text{revolutions}}{\text{minute}}\right) \cdot \left(\frac{2\pi \text{ radians}}{1 \text{ revolution}}\right) = \left(3519.8 \frac{\text{radians}}{\text{minute}}\right) \text{ (since 1 rev. = } 2\pi \text{ radians)}$$