Find the equation of a logarithm function given two points and the value of its vertical asymptote y = A log(x + B) + C

Important: One point should make the function argument (x + b) equal to 1. Steps:

- 1. Look for the value of the vertical asymptote on the graph. This gives us the vertical asymptote, set X B = 0. This gives the B value.
- 2. Look for reflection to the y axis. If the graph shows reflection, multiply the function argument (x + b) by (-1).
- 3. Find C by using the point that makes the argument(x + B) equal to 1. Therefore, Alog(x + B) will be zero and C will be the value of y.
- 4. Substitute the coordinates of a second point from the graph into the function equation to find A. It will be A = (y C)/log(x + B)
- 5. Rewrite the function equation in replacing A, B, and C with the values that were found.

Example1: Find the equation of the function for the graph below passing through (2,0), (1,2).

Solution: The general equation is y = A log(x + B) + C

1. The graph shows a vertical asymptote at x = 3. Therefore, B is given by x + 3 = 0. B = -3 the new equation is $y = A \log(x - 3) + C$

2. The graph displays a reflection to the y axis. The function is $y = A \log(-x + 3)$. The argument (x - 3) was multiplied by (-1).

3. Now substitute (2,0) (choose the x value that makes the log argument equal to 1 for simplification) into the equation:

$$0 = A \log(-2 + 3) + C,$$

$$0 = A \log(1) + C.$$

therefore, $C = 0.$

The equation becomes: $y = A \log(-x + 3)$. 4. Substituting in the point (1,2):

$$2 = A \log (-1 + 3),$$

2 = A log (2).
Then A = 2/log (2).

5. The final equation of the function is: y = 2/log(2) * log(-x + 3).



Example 2: Using the following graph, find the equation of the logarithm function passing through (-1,1) and (0, 2).

Solution: The general equation is

 $y = A \log(x + B) + C$

- 1. The graph displays a Vertical Asymptote at x = -2. Thus setting x - (-2) = 0, gives us a B value of 2. The new equation is $y = A \log(x + 2) + C$
- 2. No reflection was observed on the graph. Therefore, no change in the equation inside the parenthesis.



3. Now substitute (-1,1) (choose the x value that makes the log argument equal to 1 for simplification) into the equation that we have so far.

$$1 = A \log (-1 + 2) + C,$$

$$1 = A \log (1) + C; \text{ since } \log (1) = 0, \text{ Therefore, } C$$

$$= 1.$$

The new equation is $y = A \log(x + 2) + 1$

4. By substituting (0, 2) in the equation, we get:

$$2 = A \log (0 + 2) + 1$$

$$1 = A \log (2)$$

$$A = (2 - 1)/\log (2),$$

$$= 1$$

$$A / \log .$$

5. The final equation is $y = 1/\log(2) * \log(x+2) + 1$

