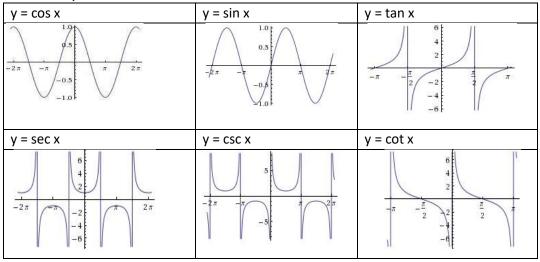
MAC 1114 – Trigonometry Basic Graphs

Basic Trigonometric Graphs:



Standard Forms

$y = a \sin k(x - b) + c y$	Amplitude= a	2π	Phase shift: b	Vertical shift: c
$= a \cos k(x - b) + c$		Period = $, k > 0$		
a 555 K(X 5) 15		k		
$y = a \csc k(x - b) + c$	Not applicable	2π	Phase shift: b	Vertical shift: c
$y = a \sec k(x - b) + c$		Period = $, k > 0$		
, a see n(x 2) 10		k		
y = a tan k(x - b) + c	Not applicable	π	Phase shift: b	Vertical shift: c
$y = a \cot k(x - b) + c$		Period = , k > 0		
, a cot(x b) . c		k		

Examples (these show one period for each example)

1. $y = 3\cos(2x + 2\pi)$: put it into the standard form by factoring out the 2 that is with the x. This gives:

$$y = 3 \cos 2(x +)$$

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Amplitude \Rightarrow 3,
$$\frac{2\pi}{2\pi}$$

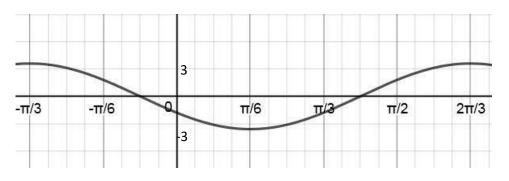
$$= \pi \text{ so would divide graph into } 0, , , -\frac{3\pi}{4} \text{ and } \pi.$$
Phase shift \Rightarrow (to the left)

5 point method: (take the unshifted graph and adjust to get new points)

Starting point: unshifted (0,3) \rightarrow (0 - $\frac{\pi}{3}$, 3)

Third point: unshifted $\binom{\pi}{2}$, -3) $\rightarrow \binom{\pi}{2} - \frac{\pi}{3}$, -3) End of period: unshifted $(\pi, 3) \rightarrow (\pi - \frac{\pi}{3}, 3)$

Second point: unshifted $\binom{\pi}{4}$, 0) \Rightarrow $\binom{\pi}{4} - \frac{\pi}{3}$, 0) Fourth point: unshifted $(\frac{3\pi}{4}, 0) \Rightarrow (\frac{3\pi}{4} - \frac{\pi}{3}, 0)$



J	
angle	value
$\frac{-\pi}{}$	3
3	
$\frac{-\pi}{}$	0
12	
$\underline{\pi}$	-3
6	
5π	0
12	
2π	3
3	

2. $y = 2 \csc(2x + \pi)$

put it into the standard form by factoring out the 2 that is with the x. This gives:

$$y = 2 \csc 2 (x + 1)$$
; period = $\frac{2\pi}{4} = \pi$ so would divide graph into $0, \frac{\pi}{7}, \frac{\pi}{7} = \frac{3\pi}{4}$ and π .

Phase shift → (to the left)

angle	value
$-\pi$	asymptote
4	

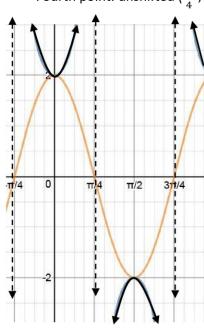
5 point method: (take the unshifted graph and adjust to get new points)

0	2	_
π	asymptote	
-		
π	-2	
<u>-</u>		
3π	asymptote	
4		

Starting point: unshifted (0,1) \rightarrow (0 $-\frac{\pi}{4}$, 1) Third point: unshifted $\binom{\pi}{2}$, -1 \rightarrow $\binom{\pi}{2} - \frac{\pi}{4}$, 0) End of period: unshifted $(\pi, 1) \rightarrow (\pi - \frac{\pi}{4}, 1)$ Second point: unshifted $\binom{\pi}{4}$, 0) $\rightarrow \binom{\pi}{4} - \frac{\pi}{4}$, 0) Fourth point: unshifted $(\frac{3\pi}{4}, 0) \rightarrow \binom{3\pi}{4} - \frac{\pi}{4}$, 0)

Hint: start with a sine graph with the same amplitude, shift and period, and the use it to graph it's inverse: the csc. The zero's become the asymptotes for the csc graph.

divide the graph into increments of like normal.



Phase shift →

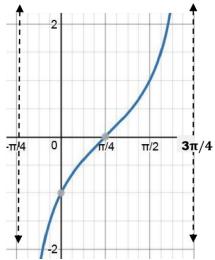
3. y =tan (x - π) Period: no change

since k = $1 \rightarrow \pi$ so

4

Starting point: unshifted $(\frac{-\pi}{2}, -\infty) \rightarrow (\frac{-\pi}{2} + \frac{\pi}{4}, -\infty)$ Second point: unshifted $(-\frac{\pi}{4}, -1) \rightarrow (-\frac{\pi}{4} + \frac{\pi}{4}, -1)$ Third point: unshifted $(0, 0) \rightarrow (0 + \frac{\pi}{4}, 0)$ Fourth point: unshifted $(\frac{\pi}{4}, 1) \rightarrow (\frac{\pi}{4} + \frac{\pi}{4}, 1)$ End of period: unshifted $(\frac{\pi}{4}, +\infty) \rightarrow (\frac{\pi}{4} + \frac{\pi}{4}, -1)$

angle	value
$\frac{-\pi}{4}$	-∞
0	-1
$\frac{\pi}{4}$	0
$\frac{\pi}{2}$	1
$\frac{3\pi}{4}$	+∞



point method: (take the unshifted graph and adjust to get new points)

$$\pi$$
 π τ 2 2 4