

MAC 1'S
Formu Horizontal Parabola

Coni $y^2 = 4px$
 Vertex: $(0,0)$
 Focus: $(p, 0)$
 Directrix: $x = -p$
 $p > 0$: opens right
 $p < 0$: opens left
 Focal diameter = $|4p|$

Horizontal Ellipse
 $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1; a > b$

Vertical Parabola
 $x^2 = 4py$
 Vertex: $(0,0)$
 Focus: $(0, p)$
 Directrix: $y = -p$
 $p > 0$: opens up
 $p < 0$: opens down
 Focal diameter = $|4p|$

Vertical Ellipse
 $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1; b > a$

Sequences

Arithmetic Sequence	Geometric Sequence
n term th $a_n = a_1 + (n-1)d$	n term th $a_n = a_1 r^{n-1}$
Partial Sum $S_n = \frac{(a_1 + a_n)n}{2}$	Finite sum $S_n = \frac{(1 - r^n)a}{1 - r}$
Partial sum $S_n = \frac{[n(2a + (n-1)d)]}{2}$	Infinite sum $S = \frac{a}{1-r}; r < 1$

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1; b > a$$

Vertices: $(\pm a, 0)$

Major axis: $2a$

Minor axis: $2b$

Focus: $(\pm c, 0)$

$$c^2 = a^2 - b^2$$

Vertices: $(0, \pm a)$

Major axis: $2b$

Minor axis: $2a$

Focus: $(0, \pm c)$

$$c^2 = b^2 - a^2$$

Horizontal Hyperbola

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

Vertices: $(\pm a, 0)$

Transverse: $2a$

Asymptotes: $y = \pm \frac{b}{a}x$

Vertical Hyperbola

$$\frac{y^2}{a^2} - \frac{x^2}{b^2} = 1$$

Vertices: $(0, \pm a)$

Transverse: $2a$

Asymptotes: $y = \pm \frac{a}{b}x$

Focus: $(\pm c, 0)$
 $c^2 = a^2 + b^2$

Focus: $(0, \pm c)$

$$c^2 = a^2 + b^2$$

Radius: r , Center: (h, k)

Circle (ellipse $a = b$)

$$(x - h)^2 + (y - k)^2 = r^2$$

Rational Functions

$$f(x) = \frac{ax^n}{bx} + \dots + \dots$$

1. x-intercept: set top = 0.
2. y-intercept: let x = 0.
3. Vertical asymptotes of $f(x)$ are the zeros of the denominator.
4. if $n < m$, horizontal asymptote: $y = 0$.
5. if $n = m$, horizontal asymptote: $y = a/b$.
6. if $n > m$ then no horizontal asymptote.
7. if $n = m + 1$, find slant asymptotes by division.

Factorials- Coefficients

$$C(n, r) = \frac{n!}{r!(n-r)!}$$

Exponential Growth & Decay

$$M(t) = n_0 e^{rt}; r \text{ negative for decay}$$

$$r = \frac{\ln 2}{h}; h = \text{half-life \& doubling}$$

Partial Fractions Decomposition

$$\frac{1}{(x-a)(x-b)} = \frac{A}{x-a} + \frac{B}{x-b};$$

$$\frac{1}{(x-a)^2(x-b)} = \frac{A}{x-a} + \frac{B}{(x-a)^2} + \frac{C}{x-b};$$

$$\frac{1}{(x^2+a)(x-b)} = \frac{Ax+B}{x^2+a} + \frac{C}{x-b}$$