## Trigonometry Fundamentals and the Unit Circle

 The six trigonometric functions sine, cosine, tangent, cosecant, secant, cotangent are derived from relationships with right triangles. Common values result from two right triangles:
$\sin \left(30^{\circ}\right)=\frac{\text { OPP }}{\text { HYP }}=\frac{1}{2}$
$\cos \left(30^{\circ}\right)=\frac{\text { ADJ }}{\text { HYP }}=\frac{\sqrt{3}}{2}$
$\tan \left(30^{\circ}\right)=\frac{\text { OPP }}{\text { ADJ }}=\frac{1}{\sqrt{3}}=\frac{\sqrt{3}}{3}$
(Note: values for $60^{\circ}$ are found similarly.)

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$$
\begin{aligned}
& \sin \left(45^{\circ}\right)=\frac{\text { OPP }}{\text { HYP }}=\frac{1}{\sqrt{2}}=\frac{\sqrt{2}}{2} \\
& \cos \left(45^{\circ}\right)=\frac{\text { ADJ }}{\text { HYP }}=\frac{1}{\sqrt{2}}=\frac{\sqrt{2}}{2} \\
& \tan \left(45^{\circ}\right)=\frac{\text { OPP }}{\text { ADJ }}=\frac{1}{1}=1
\end{aligned}
$$

"All Students Take Calculus"
"SOH CAH TOA"


ADJ

SOH $\sin \theta=\frac{\text { OPP }}{\text { HYP }}$

CAH $\cos \boldsymbol{\theta}=\frac{\text { ADJ }}{\text { HYP }}$
TOA $\tan \boldsymbol{\theta}=\frac{\mathrm{OPP}}{\mathrm{ADJ}}$
$\boldsymbol{s e c} \boldsymbol{\theta}=\frac{\mathrm{HYP}}{\mathrm{ADJ}}$
$\cot \boldsymbol{\theta}=\frac{\mathrm{ADJ}}{\mathrm{OPP}}$
$\boldsymbol{\operatorname { c s c }} \boldsymbol{\theta}=\frac{\mathrm{HYP}}{\mathrm{OPP}}$

| Take |
| :---: | :---: |
| Tan positive |
| sin: - |
| $\cos :-$ |
| $\tan :+$ |
| Cos positive |
| sin: - |
| $\cos :+$ |
| $\tan :-$ |

The Unit Circle - the center at the origin; a radius of 1. Coordinates of $(\cos \theta, \sin \theta)$


